Calculating interface resistance

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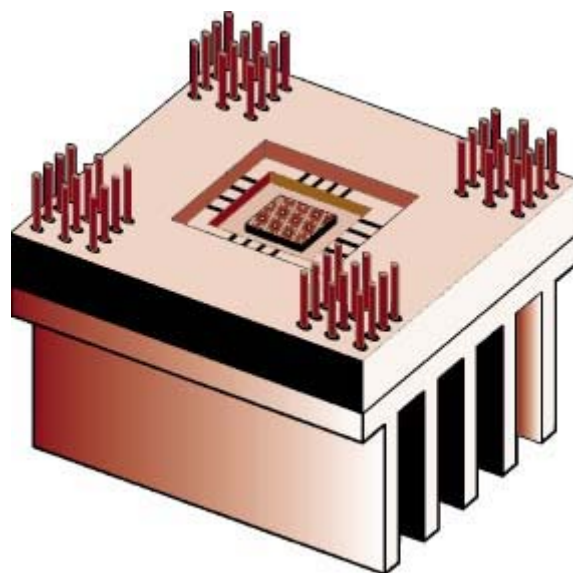
Figure 1. Ceramic Package - Aluminum Heat Sink Assembly

Introduction

The exposed surface area of many of today's high powered electronic packages is no longer sufficient for the removal of the heat generated during normal operation. Heat sinks are a commonly-used, low cost means of increasing the effective surface area for dissipating heat by means of convective air cooling. While the use of a heat sink lowers the fluid-side thermal resistance, it also introduces an interface resistance across the contact formed between itself and the package case. Under some circumstances, this contact resistance can be substantial, impeding heat flow and reducing the overall effectiveness of the heat sink. Figure 1 depicts an electronic package heat sink assembly which would typically be joined by plastic or metal spring clips around the perimeter of the assembly.

The subject of thermal resistance at interfaces between aluminum heat sinks and ceramic packages has been discussed by Lee [1], de Sorgo [2], Latham [3] and Early et al. [4]. These articles primarily report test results for joint resistance as a function of contact

pressure for various interface types. The interfaces examined in these works involve either bare surfaces (air filled) or joints where the interstitial gap is filled with a material layer containing dispersed thermally conductive fillers. Interstitial material layers currently used by the industry, as described by de Sorgo [2], include thermal greases, thermally conductive compounds, elastomers, and adhesive tapes.
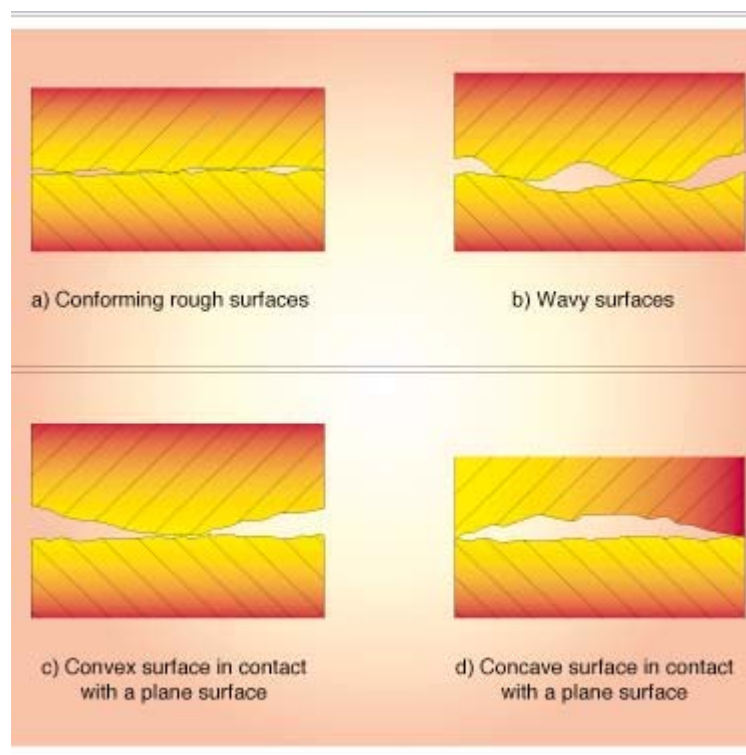

Figure 2. Contact Configurations

The objective of this article is to illustrate how to calculate the thermal joint resistance for the interface formed by two conforming, rough surfaces shown in Figure 2a, as a function of contact pressure for the low pressure range, between 0.035 and 0.35 *Mpa (5 and 50 psi)*, commonly encountered in microelectronic applications (Latham [3]). Peterson and Fletcher [5] verified by experiments in vacuum that the following models, which were originally developed for metal-to-metal contacts, give very good results when used to predict the contact conductance at interfaces formed by metals (invar, kovar and alloy 42) and mold compounds (polyset 410B and 410C, MG25F-LMP and MG45F-04) at the interface temperature range: 20 °C to 70 °C and the interface pressure range: 0.5 to 5.0 *MPa*. This work will focus primarily on bare joints, although an example where the interface material is treated as a liquid, such as in the case of a thermal grease, will also be considered. Interfaces with thermal compounds or elastomeric sheet materials will be shown to be very difficult to model and will be discussed in general terms only. The non-conforming wavy, convex or concave interfaces depicted in Figures 2b, 2c, and 2d, respectively, are exceedingly complex to model and therefore will not be considered here. Since radiation heat transfer at most interfaces is negligible or non-existent, it will not be included in this analysis.

Conforming rough surface model

The thermal joint conductance, h_j, of the interface formed by two conforming, rough surfaces is given by the following simple model proposed by Yovanovich [6] and further described and used by Antonetti and Yovanovich [7], Yovanovich and Antonetti [8], an and Yovanovich [9].

$$h_j = h_c + h_g$$

The contact conductance is given by:

$$h_c = 1.25\, k_s \frac{m}{\sigma}\left(\frac{P}{H_c}\right)^{0.95}$$

where k_s is the harmonic mean thermal conductivity of the interface:

$$k_s = 2\, k_1 k_2 /(k_1 + k_2)$$

the effective mean absolute asperity slope of the interface m, as shown in Figure 3, is given by:

$$m = \sqrt{m_1^2 + m_2^2}$$

and where σ, also shown in Figure 3, is the effective RMS surface roughness of the contacting asperities:

$$\sigma = \sqrt{\sigma_1^2 + \sigma_2^2}$$

The contact pressure is P and H_c is the *surface* microhardness of the softer of the two contacting solids. The microhardness is in general complex because it depends on several geometric and physical parameters, such as the Vickers microhardness correlation coefficients.

The surface asperity slope is frequently not given. In this case the mean absolute asperity slope can be approximated by the correlation equation proposed by Antonetti et al. [10]:

$$m = 0.125\, (\sigma \times 10^6)^{0.402}$$

which was developed for the surface roughness range:

$$0.216\, \mu\, m \leq \sigma < 9.6\, \mu\, m$$

The gap conductance, h_g, is given by the approximation of Yovanovich [6]:

$$h_g = k_g/(Y + M)$$

where kg is the thermal conductivity of the gap substance. The effective gap thickness Y, shown in Figure 3, can be calculated accurately by means of the simple power-law correlation equation proposed by Antonetti and Yovanovich [7]:

$$Y = 1.53\, \sigma\, (P/H_c)^{-0.097}$$

for the relative contact pressure range:
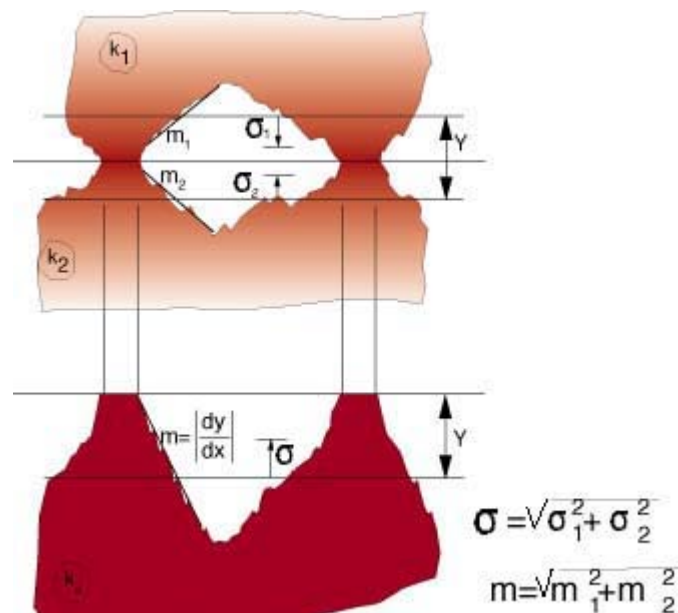
$$10^{-5} < P/H_c < 2 \times 10^{-2}.$$

Figure 3. Conforming rough surfaces

The gas parameter M accounts for rarefaction effects at high temperatures and low gas pressures. This gas-surface parameter depends on the thermal accommodation coefficients, the ratio of specific heats, the Prandtl number, and the molecular mean free-path of the gas. Song and Yovanovich [11] present correlation equations for the calculation of the accommodation coefficients for several gases as a function of the gas temperature. This complex gas-surface parameter depends on gas pressure and temperature according to the relationship:

$$M = M_0 \frac{T}{T_0} \frac{P_{g,0}}{P_g}$$

where M_0 denotes the gas parameter value at the reference values of gas temperature and pressure, T_0 and $P_{g,0}$, respectively. Reference values of the gas parameter for air and helium are presented in Table 1.

Table 1: Thermophysical Properties of Gap Substances

Gap Substance	Thermal Conductivity $W/(mK)$	Gas Parameter M_0 x 10^6, m
air	0.026	0.373**
helium	0.150	2.05**
thermal grease	0.20 - 0.70*	0.0
doped thermal grease	1.68 - 2.58*	0.0

** - T_0 - 50 °C, $P_{g,0}$ = 1 *atm*

* - AOS Technical Data Sheets, 1995

Interstitial material layers

Although the conforming rough surface model presented in the previous section was developed for bare surfaces, it can also be applied to interfaces with thermal grease. By assuming that the grease behaves as a liquid and fills all gaps between the contacting asperities, the existing model can be used by substituting $M = 0$ and the thermal conductivity of the grease into the gap conductance relationship. However, when solid interstitial materials are used, such as thermal compounds, elastomers or adhesive tapes, the joint conductance problem becomes much more complicated. As shown in Figure 4, the use of a solid interstitial material introduces an additional interface to the problem.
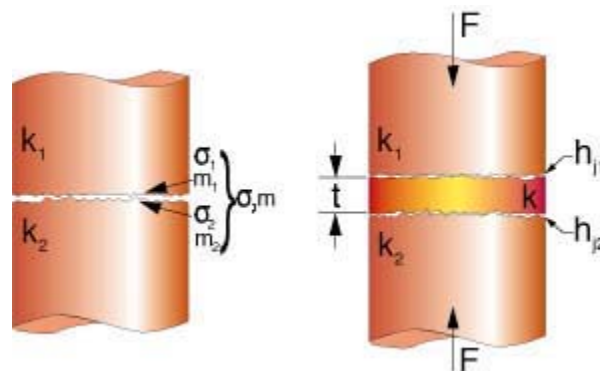

Figure 4. Thermal conductance across an interface with and without an interstitial material

Using thermal resistance concepts, the overall joint conductance for this problem is determined by the series combination:

$$1/h_j = 1/(h_j,1) + t/k + 1/(h_j,2)$$

where $h_{j,1}$ and $h_{j,2}$ refer to the joint conductance between each of the contacting surfaces and the interfacial material and t and k are the average thickness and thermal conductivity of the layer. Completing this analysis requires characterization of the relevant surface parameters, such as the slope, roughness and microhardness, for the various interstitial materials. In addition, for elastomeric materials the layer thickness t is not constant but instead depends on the contact pressure. Additional research needs to be done before a model can be developed to address this complex phenomenon.

Application to aluminum heat sink-ceramic package interface

Table 2: Thermal and Surface Properties for Aluminum-Alumina Conforming Rough Surfaces

Material	Thermal Conductivity W/(m K)	Microhardness MPa	Surface Roughness μ m
A1 5052 [14]	140	745	6.9
A1 6061 [14]	180	705	0.7
A1 6063-T5	201	1094	0.4 (flycut)
Aluminum Nitride [13]	160	10044	0.45
Alumina (96% Al_2O_3)	20.9	3100	1.3 (ground)
Copper [13]	397	924.1	0.45 (milled)

The aforementioned models will be used to calculate the joint resistances for the interface formed by an aluminum 6063-T5 aluminum heat sink and Al_2O_3 alumina package. The thermal conductivities of the heat sink and ceramic package are k_1 = 201 $W/m·K$ and k_2 = 20.9 $W/m·K$ respectively. The harmonic mean thermal conductivity of the interface is k_s = 37.85 $W/m·K$. Since the microhardness of the aluminum alloy is 1094 MPa, which is much less than that of the alumina, it will be used to compute the contact parameters. Based on a surface roughness for flycut aluminum of σ_1 = 0.4 μm and a surface roughness for ground alumina of σ_2 = 1.3 μm, the effective surface roughness of the interface is calculated as σ = 1.36 μm. Since the surface slopes are not given, Eq. (6) will be used to calculate the following values: m_1 = 0.139, m_2 = 0.0865, respectively. The effective surface slope of the interface is therefore m = 0.164. The thermal and physical properties of air, helium and grease presented in Table 1 will be used in the gap conductance model.

In Figure 5 the joint thermal resistances, whose units are $cm^{2-°}C/W$ are plotted against

the nominal contact pressure over the pressure range: $0.007 \leq P \, (Mpa) \leq 0.35$ for several cases. The bare joint resistances with air or helium present in the gap are shown. The effect of a thermal grease of thermal conductivity $k_g = 0.20 \, W/m{\cdot}K$ is also shown in Figure 5.
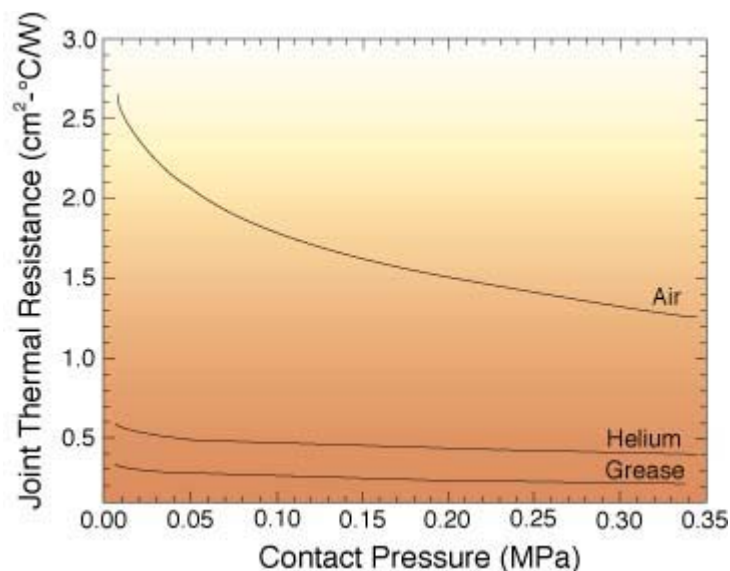

Figure 5. Joint thermal resistance of an aluminum heat sink-ceramic package assembly for various contact pressures

Summary and discussion

Simple correlation equations are presented and used to calculate thermal joint resistances for a typical aluminum-ceramic interface found in microelectronics applications. Flycut and ground surfaces are considered. Joint resistances are calculated for contact pressures between 0.007 and 0.35 *MPa*, which includes the practical microelectronic pressure range of 0.07 and 0.17 *Mpa* (see Latham [3]). The greatest joint resistances are found when air is present in the interstitial gap. In the contact pressure range of 0.007 to 0.35 *MPa*, the air joint resistance goes from 2.665 to 1.903 $cm^{2-\circ}C/W$.

When silicon grease is placed in the gap, the joint resistance is much smaller than the bare interface. The calculated values of the joint resistance lie in the range 0.335 to 0.213 $cm^{2-\circ}C/W$ which are an order of magnitude smaller than the joint resistances of a bare joint. If greases with thermally conductive ceramics are used, the joint resistance can be reduced to values below 0.065 $cm^{2-\circ}C/W$.

The correlation equations which have been used are based on conforming rough surfaces with interstitial substances which perfectly wet all portions of the surfaces which form the gap. Any non-flatness will result in interfaces with larger gaps which will have larger joint resistances. If the interstitial substance does not perfectly *wet* the contacting surfaces, this will also produce a more thermally resistive interface. The proposed models

and correlation equations therefore correspond to the best thermal joints which have the smallest joint resistances.

The use of other interstitial materials, such as thermal compounds, elastomers or adhesive tapes, has been shown to increase the complexity of the joint conductance problem significantly. In order to successfully model this problem, extensive research into characterizing the surface properties and layer thicknesses for the various interfacial materials is required.

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